

Fraction Volume Quest

Find prism volume with fractional measurements.

GRADE 6 • 6.G.A.2

CCSS.Math.Content.6.G.A.2 "Find the volume of a right rectangular prism with fractional edge lengths by packing it with unit cubes of the appropriate unit fraction edge lengths..."

NAME _____

DATE _____

MULTIPLY THE THREE EDGES

For a right rectangular prism, multiply length, width, and height: $V = l \times w \times h$. You can also find the base area first, $b = l \times w$, then use $V = b \times h$. Packing with cubes whose edge length is a common unit fraction gives the same total volume.

WORKED EXAMPLE

Find the volume of a right rectangular prism with length $\frac{5}{6}$ unit, width $\frac{7}{10}$ unit, and height $\frac{9}{8}$ unit.

1. Find the base area: $b = \frac{5}{6} \times \frac{7}{10} = \frac{7}{12}$ square unit.
2. Multiply the base area by the height: $V = \frac{7}{12} \times \frac{9}{8}$.
3. Simplify: $V = \frac{21}{32}$ cubic unit.

Answer: $\frac{21}{32}$ cubic unit

PRACTICE 6 problems

- 1** A prism is $\frac{3}{4}$ unit long, $\frac{1}{2}$ unit wide, and $\frac{1}{4}$ unit high. It is packed with cubes that each have an edge length of $\frac{1}{4}$ unit. How many small cubes fit? What is the prism's volume?

ANSWER _____

- 2** Find the volume of a prism with length $\frac{7}{9}$ unit, width $\frac{3}{5}$ unit, and height $\frac{3}{2}$ units.

ANSWER _____

- 3** A prism has length $\frac{4}{7}$ unit and width $\frac{7}{8}$ unit. Its volume is $\frac{3}{8}$ cubic unit. Find its height.

ANSWER _____

- 4** Find the volume of a prism with length $\frac{5}{12}$ unit, width $\frac{6}{11}$ unit, and height $\frac{11}{10}$ units.

ANSWER _____

- 5** The base area of a right rectangular prism is $\frac{13}{15}$ square unit. Its height is $\frac{15}{26}$ unit. Find the volume.

ANSWER _____

- 6** Find the volume of a prism with length $\frac{2}{5}$ unit, width $\frac{3}{7}$ unit, and height $\frac{5}{6}$ unit.

ANSWER _____

APPLY IT Show your work

- 1** The gaming club is making a solid rectangular prize block for a tournament. The block is $1\frac{1}{2}$ inches long, $\frac{2}{3}$ inch wide, and $\frac{3}{5}$ inch high. How much material is in the block?

WORK SPACE

ANSWER _____

- 2** A school garden has a rectangular planter box that is $\frac{7}{8}$ yard long, $\frac{4}{9}$ yard wide, and $1\frac{1}{2}$ yards high. What is the volume inside the planter box?

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

A prism is $\frac{3}{2}$ units long, $\frac{4}{3}$ units wide, and $\frac{5}{4}$ units high. Use cubes with edge length $\frac{1}{12}$ unit to show that packing and multiplying give the same volume. State the number of cubes and the volume.

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	A prism is $\frac{3}{4}$ unit long, $\frac{1}{2}$ unit wide, and $\frac{1}{4}$ unit high. It is packed with cubes that each have an edge length of $\frac{1}{4}$ unit. How many small cubes fit? What is the prism's volume?	6 small cubes; $\frac{3}{32}$ cubic unit
2	Find the volume of a prism with length $\frac{7}{9}$ unit, width $\frac{3}{5}$ unit, and height $\frac{3}{2}$ units.	$\frac{7}{10}$ cubic unit
3	A prism has length $\frac{4}{7}$ unit and width $\frac{7}{8}$ unit. Its volume is $\frac{3}{8}$ cubic unit. Find its height.	$\frac{3}{4}$ unit
4	Find the volume of a prism with length $\frac{5}{12}$ unit, width $\frac{6}{11}$ unit, and height $\frac{11}{10}$ units.	$\frac{1}{4}$ cubic unit
5	The base area of a right rectangular prism is $\frac{13}{15}$ square unit. Its height is $\frac{15}{26}$ unit. Find the volume.	$\frac{1}{2}$ cubic unit
6	Find the volume of a prism with length $\frac{2}{5}$ unit, width $\frac{3}{7}$ unit, and height $\frac{5}{6}$ unit.	$\frac{1}{7}$ cubic unit

PART 2 • APPLY IT

- $\frac{3}{5}$ cubic inch** Convert $1\frac{1}{2}$ to $\frac{3}{2}$. Then multiply: $\frac{3}{2} \times \frac{2}{3} \times \frac{3}{5} = \frac{3}{5}$.
- $\frac{7}{12}$ cubic yard** Find the base area: $\frac{7}{8} \times \frac{4}{9} = \frac{7}{18}$ square yard. Multiply by the height: $\frac{7}{18} \times \frac{3}{2} = \frac{7}{12}$.

CHALLENGE

The prism holds $18 \times 16 \times 15 = 4,320$ cubes. Each cube has volume $\frac{1}{1728}$ cubic unit, so $4,320 \times \frac{1}{1728} = \frac{5}{2}$ cubic units. Multiplying the edges also gives $\frac{3}{2} \times \frac{4}{3} \times \frac{5}{4} = \frac{5}{2}$ cubic units.

Accept equivalent fractions and mixed-number forms when correct. For the packing problem and challenge, accept correct cube counts paired with the matching total volume.