

Line Link Lab

Connect rates, graphs, and equations.

GRADE 8 • 8.EE.B

CCSS.Math.Content.8.EE.B "Understand the connections between proportional relationships, lines, and linear equations."

NAME _____

DATE _____

THE BIG IDEA

A proportional relationship has a constant ratio y/x and can be written as $y = mx$. Its graph is a line through $(0,0)$, and m is both the unit rate and the slope. A linear equation $y = mx + b$ is also a line, but it is proportional only when $b = 0$.

WORKED EXAMPLE

A proportional relationship includes the point $(11, 88)$. Write its equation and identify its slope.

1. Find the unit rate: $88/11 = 8$.
2. Use $y = mx$ because a proportional line goes through $(0,0)$.
3. Substitute $m = 8$: $y = 8x$.

Answer: $y = 8x$; slope = 8

PRACTICE 6 problems

- 1** The table shows x -values 2, 4, and 6 with y -values 10, 20, and 30. Is the relationship proportional? Write its equation.

ANSWER _____

- 2** For $y = -3x$, state the slope and tell whether the relationship is proportional.

ANSWER _____

- 3** For $y = 4x + 9$, state the slope, the y -intercept, and whether the relationship is proportional.

ANSWER _____

- 4** A line passes through $(0,0)$ and $(5,-15)$. Write its equation.

ANSWER _____

- 5** The table has points $(1,6)$, $(2,12)$, and $(3,19)$. Is the relationship proportional? Explain using ratios.

ANSWER _____

- 6** Compare $y = 2x$ and $y = 2x + 5$. Do they have the same slope? Are they both proportional?

ANSWER _____

APPLY IT Show your work

- 1** A music app has two plans. Plan A costs \$5 per month plus a one-time \$12 setup fee. Plan B costs \$7 per month with no setup fee. Let x be the number of months and y be the total cost. Write an equation for each plan. After how many months do the plans cost the same amount?

WORK SPACE

ANSWER _____

- 2** At a school esports event, volunteers earn 14 prize tokens for 2 hours of work. The number of tokens is proportional to the number of hours. Let x be hours and y be tokens. Write an equation and find the number of tokens earned after 9 hours.

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

Line A has equation $y = -2x + 6$. Line B passes through $(0,6)$ and $(3,0)$. Are the two lines the same line? Explain your reasoning.

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	The table shows x-values 2, 4, and 6 with y-values 10, 20, and 30. Is the relationship proportional? Write its equation.	Yes; $y = 5x$.
2	For $y = -3x$, state the slope and tell whether the relationship is proportional.	Slope = -3; yes, it is proportional.
3	For $y = 4x + 9$, state the slope, the y-intercept, and whether the relationship is proportional.	Slope = 4; y-intercept = 9; it is not proportional.
4	A line passes through (0,0) and (5,-15). Write its equation.	$y = -3x$
5	The table has points (1,6), (2,12), and (3,19). Is the relationship proportional? Explain using ratios.	No; $6/1 = 6$ and $12/2 = 6$, but $19/3$ is not 6.
6	Compare $y = 2x$ and $y = 2x + 5$. Do they have the same slope? Are they both proportional?	They have the same slope, 2. Only $y = 2x$ is proportional.

PART 2 • APPLY IT

- Plan A: $y = 5x + 12$. Plan B: $y = 7x$. They cost the same after 6 months, when each costs \$42.** Set the total costs equal: $5x + 12 = 7x$. This gives $x = 6$, and substituting gives a total cost of \$42.
- $y = 7x$; 63 tokens** The unit rate is $14/2 = 7$ tokens per hour, so $y = 7x$. Substitute $x = 9$ to get $y = 63$.

CHALLENGE

Yes. The slope of Line B is $(0 - 6)/(3 - 0) = -2$, and its y-intercept is 6, so both lines have equation $y = -2x + 6$.

Accept equivalent equation forms, such as $3x + y = 0$ for $y = -3x$. For proportionality explanations, require evidence of a constant ratio or a y-intercept of 0.