

Volume Vault

Find exact volumes with pi.

GRADE 8 • 8.G.C

CCSS.Math.Content.8.G.C "Solve real-world and mathematical problems involving volume of cylinders, cones, and spheres."

NAME _____

DATE _____

VOLUME RULES

For a cylinder, multiply pi x radius squared x height. For a cone, take 1/3 of that product, and for a sphere use $\frac{4}{3} \times \pi \times \text{radius cubed}$. If you are given a diameter, divide it by 2 to find the radius, and write volume in cubic units.

WORKED EXAMPLE

Find the volume of a cylinder with radius 2 cm and height 11 cm.

1. Use $V = \pi r^2 h$.
2. $V = \pi(2^2)(11)$.
3. $V = \pi(4)(11) = 44\pi$.

Answer: $44\pi \text{ cm}^3$

PRACTICE 6 problems

- 1** Find the volume of a cylinder with radius 3 cm and height 5 cm.

ANSWER _____

- 2** Find the volume of a cone with radius 6 cm and height 8 cm.

ANSWER _____

- 3** Find the volume of a sphere with radius 3 cm.

ANSWER _____

- 4** Find the volume of a cylinder with diameter 10 cm and height 6 cm.

ANSWER _____

- 5** Find the volume of a cone with diameter 12 cm and height 9 cm.

ANSWER _____

- 6** Find the volume of a sphere with radius 5 cm.

ANSWER _____

APPLY IT Show your work

- 1** The robotics club is making 5 identical cone-shaped resin trophy tops. Each top has a radius of 3 cm and a height of 12 cm. What total volume of resin is needed?

WORK SPACE

ANSWER _____

- 2** A refillable water bottle has a cylindrical space inside with radius 5 cm and height 12 cm. What is the bottle's capacity in cubic centimeters?

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

A custom container is made from a cylinder with a hemispherical cap on top. Both parts have radius 6 cm, and the cylinder is 10 cm tall. What is the total volume of the container?

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	Find the volume of a cylinder with radius 3 cm and height 5 cm.	$45\pi \text{ cm}^3$
2	Find the volume of a cone with radius 6 cm and height 8 cm.	$96\pi \text{ cm}^3$
3	Find the volume of a sphere with radius 3 cm.	$36\pi \text{ cm}^3$
4	Find the volume of a cylinder with diameter 10 cm and height 6 cm.	$150\pi \text{ cm}^3$
5	Find the volume of a cone with diameter 12 cm and height 9 cm.	$108\pi \text{ cm}^3$
6	Find the volume of a sphere with radius 5 cm.	$500\pi/3 \text{ cm}^3$

PART 2 • APPLY IT

- $180\pi \text{ cm}^3$** One cone has volume $\frac{1}{3} \times \pi \times 3^2 \times 12 = 36\pi \text{ cm}^3$. Multiply 36π by 5 trophy tops.
- $300\pi \text{ cm}^3$** Use $V = \pi r^2 h$. Substitute the radius and height: $\pi \times 5^2 \times 12 = 300\pi$.

CHALLENGE

 $504\pi \text{ cm}^3$

Accept equivalent exact forms, such as $(500\pi)/3 \text{ cm}^3$. For the challenge, accept work that adds $360\pi \text{ cm}^3$ for the cylinder and $144\pi \text{ cm}^3$ for the hemisphere.