

Matrix Matchup

Turn systems into one organized equation.

HIGH SCHOOL • HSA-REI.C.8

CCSS.Math.Content.HSA-REI.C.8 "(+) Represent a system of linear equations as a single matrix equation in a vector variable."

NAME _____

DATE _____

BUILD THE MATRIX EQUATION

Put each equation in the same variable order, then place its coefficients in one row of a matrix. Put the variables in a column vector and the constants in a second column vector. Use 0 when a variable is missing from an equation.

WORKED EXAMPLE

Write this system as one matrix equation: $13x - 14y = 15$; $16x + 17y = 19$.

1. Use the x and y coefficients from the first equation for the first row: $[13 \ -14]$.
2. Use the x and y coefficients from the second equation for the second row: $[16 \ 17]$.
3. Place $[x; y]$ beside the coefficient matrix and place the constants in a column vector.

Answer: $[13 \ -14; 16 \ 17][x; y] = [15; 19]$

PRACTICE 6 problems

- 1** Write this system as one matrix equation: $2x + y = 6$; $-x + 3y = 9$.

ANSWER _____

- 2** Write this system as one matrix equation: $6x - 2y = 10$; $-x + 9y = 12$.

ANSWER _____

- 3** Write this system as one matrix equation: $y = 2x + 6$; $10x + y = 12$.

ANSWER _____

- 4** Write this system as one matrix equation: $2a - b + c = 9$; $a + 6b - 2c = 1$; $-a + 2b + 10c = 12$.

ANSWER _____

- 5** Write this system as one matrix equation: $x - y = 2$; $6y = 10$.

ANSWER _____

- 6** Write this system as one matrix equation: $3m + 2n = 1$; $-m + 10n = 6$.

ANSWER _____

APPLY IT Show your work

- 1** At a music festival, a ticket costs x dollars and a snack voucher costs y dollars. Maya buys 2 tickets and 6 vouchers for \$18. Jordan buys 10 tickets and 1 voucher for \$22. Write a matrix equation for the two purchases.

WORK SPACE

ANSWER _____

- 2** An esports club rents gaming PCs for x dollars each and headsets for y dollars each. For practice, it rents 12 PCs and 2 headsets for \$68. For a tournament, it rents 6 PCs and 10 headsets for \$62. Write a matrix equation for the rental costs.

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

Write this system as one matrix equation. Then explain why the coefficient matrix has 3 columns: $x + 2y - z = 6$; $-2x + 6y + z = 12$; $10x - y + 2z = 18$.

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	Write this system as one matrix equation: $2x + y = 6$; $-x + 3y = 9$.	$[2 \ 1; -1 \ 3][x; y] = [6; 9]$
2	Write this system as one matrix equation: $6x - 2y = 10$; $-x + 9y = 12$.	$[6 \ -2; -1 \ 9][x; y] = [10; 12]$
3	Write this system as one matrix equation: $y = 2x + 6$; $10x + y = 12$.	$[-2 \ 1; 10 \ 1][x; y] = [6; 12]$
4	Write this system as one matrix equation: $2a - b + c = 9$; $a + 6b - 2c = 1$; $-a + 2b + 10c = 12$.	$[2 \ -1 \ 1; 1 \ 6 \ -2; -1 \ 2 \ 10][a; b; c] = [9; 1; 12]$
5	Write this system as one matrix equation: $x - y = 2$; $6y = 10$.	$[1 \ -1; 0 \ 6][x; y] = [2; 10]$
6	Write this system as one matrix equation: $3m + 2n = 1$; $-m + 10n = 6$.	$[3 \ 2; -1 \ 10][m; n] = [1; 6]$

PART 2 • APPLY IT

1. $[2 \ 6; 10 \ 1][x; y] = [18; 22]$ Use x for the ticket cost and y for the voucher cost. Each purchase gives one row of coefficients, and the total cost goes in the constants vector.
2. $[12 \ 2; 6 \ 10][x; y] = [68; 62]$ Use the number of PCs and headsets as the coefficients in each row. Put the two rental totals in the column vector on the right.

CHALLENGE

$[1 \ 2 \ -1; -2 \ 6 \ 1; 10 \ -1 \ 2][x; y; z] = [6; 12; 18]$. The coefficient matrix has 3 columns because each row needs one coefficient for x , y , and z .

Accept equivalent matrix equations when the variable order is consistent across the coefficient matrix and variable vector. If a variable is missing from an equation, require a 0 in its matrix position.