

Function Mashups

Build one function inside another.

HIGH SCHOOL • HSF-BF.A.1c

CCSS.Math.Content.HSF-BF.A.1c "(+) Compose functions. For example, if $T(y)$ is the temperature in the atmosphere as a function of height, and $h(t)$ is the height of a weather balloon as a function of time..."

NAME _____

DATE _____

THE BIG IDEA

To find $f(g(x))$, apply g first, then use that output as the input of f . Replace every x in $f(x)$ with $g(x)$, then simplify. The order matters because $f(g(x))$ is usually not equal to $g(f(x))$.

WORKED EXAMPLE

Let $f(x)=8x-5$ and $g(x)=x^2+6$. Find $f(g(x))$.

1. $f(g(x))=8g(x)-5$

2. $=8(x^2+6)-5$

3. $=8x^2+48-5$

4. $=8x^2+43$

Answer: $f(g(x))=8x^2+43$

PRACTICE 6 problems

1 Let $f(x)=2x+7$ and $g(x)=x-4$. Find $f(g(x))$.

ANSWER _____

2 Let $p(x)=x^2-3$ and $q(x)=2x$. Find $p(q(x))$.

ANSWER _____

3 Let $m(x)=7-x$ and $n(x)=x+9$. Find $m(n(x))$.

ANSWER _____

4 Let $a(x)=3x$ and $b(x)=x^2-1$. Find $b(a(x))$.

ANSWER _____

5 Let $r(x)=4x+2$ and $s(x)=3-x$. Find $r(s(x))$.

ANSWER _____

6 Let $u(x)=x/2+7$ and $v(x)=4x-3$. Find $u(v(x))$.

ANSWER _____

APPLY IT Show your work

1

A gaming channel's number of followers, in hundreds, is $F(v)=3v+2$, where v is its number of posted videos. The channel posts $V(w)=7w+4$ videos after w weeks. Write $F(V(w))$ and state what it represents.

WORK SPACE

ANSWER _____

2

For a drone video project, the temperature at h kilometers above ground is $T(h)=31-4h$ degrees Celsius. The drone's height after t minutes is $H(t)=3t+2$ kilometers. Write $T(H(t))$ and state what it represents.

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

Let $f(x)=2x-1$ and $g(x)=x^2+4$. Solve $f(g(x))=9$.

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	Let $f(x)=2x+7$ and $g(x)=x-4$. Find $f(g(x))$.	$f(g(x))=2x-1$
2	Let $p(x)=x^2-3$ and $q(x)=2x$. Find $p(q(x))$.	$p(q(x))=4x^2-3$
3	Let $m(x)=7-x$ and $n(x)=x+9$. Find $m(n(x))$.	$m(n(x))=-x-2$
4	Let $a(x)=3x$ and $b(x)=x^2-1$. Find $b(a(x))$.	$b(a(x))=9x^2-1$
5	Let $r(x)=4x+2$ and $s(x)=3-x$. Find $r(s(x))$.	$r(s(x))=14-4x$
6	Let $u(x)=x/2+7$ and $v(x)=4x-3$. Find $u(v(x))$.	$u(v(x))=2x+11/2$

PART 2 • APPLY IT

1. $F(V(w))=21w+14$. It represents the channel's follower count, in hundreds, after w weeks. Substitute $V(w)$ for v in $F(v)$: $3(7w+4)+2=21w+14$. The input is weeks, and the output is followers in hundreds.
2. $T(H(t))=23-12t$. It represents the drone's temperature in degrees Celsius after t minutes. Substitute $H(t)$ for h in $T(h)$: $31-4(3t+2)=23-12t$. The composition gives temperature as a function of time.

CHALLENGE

$x=-1$ or $x=1$

Accept algebraically equivalent expressions, such as $14-4x$ for item 5. For word problems, require both the composed rule and a correct description of its input and output units.