

Arc Length Angles

Read radians as distances around a unit circle.

HIGH SCHOOL • HSF-TF.A.1

CCSS.Math.Content.HSF-TF.A.1 "Understand radian measure of an angle as the length of the arc on the unit circle subtended by the angle."

NAME _____

DATE _____

RADIANS ON THE UNIT CIRCLE

On a unit circle, the radian measure of a central angle equals the length of the arc it subtends. Because the radius is one unit, $s = \theta$, where s is arc length and θ is angle measure in radians.

WORKED EXAMPLE

On a unit circle, a central angle subtends an arc $11/4$ units long. Find the angle measure in radians.

1. On a unit circle, use $s = \theta$.
2. Substitute $s = 11/4$: $11/4 = \theta$.
3. The angle measures $11/4$ radians.

Answer: $11/4$ radians

PRACTICE 6 problems

- 1** An arc on a unit circle has length $3\pi/5$ units. Find the central angle in radians.

ANSWER _____

- 2** An angle measures $-7\pi/6$ radians on a unit circle. Find its signed arc length.

ANSWER _____

- 3** An arc on a unit circle has length $9/2$ units. Find the central angle in radians.

ANSWER _____

- 4** An angle measures $5\pi/3$ radians on a unit circle. Find the arc length it subtends.

ANSWER _____

- 5** An arc on a unit circle has length 2π units. Find the central angle in radians.

ANSWER _____

- 6** The minor arc subtended by a central angle on a unit circle has length $\pi/8$ units. Find the angle measure in radians.

ANSWER _____

APPLY IT Show your work

- 1** In a game design class, a student models a turn dial as a unit circle. During one move, the marker travels counterclockwise along an arc of length $13\pi/12$ units. What angle does the marker sweep, in radians?

WORK SPACE

ANSWER _____

- 2** A fitness app models its circular progress ring as a unit circle. Its marker moves clockwise through an angle of $-5\pi/8$ radians. What is the marker's signed arc length?

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

A point starts at the rightmost point of a unit circle and travels counterclockwise along an arc of length $19\pi/6$ units. State its total angle measure in radians, then find a coterminal angle between 0 and 2π . Explain your reasoning.

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	An arc on a unit circle has length $3\pi/5$ units. Find the central angle in radians.	$3\pi/5$ radians
2	An angle measures $-7\pi/6$ radians on a unit circle. Find its signed arc length.	$-7\pi/6$ units
3	An arc on a unit circle has length $9/2$ units. Find the central angle in radians.	$9/2$ radians
4	An angle measures $5\pi/3$ radians on a unit circle. Find the arc length it subtends.	$5\pi/3$ units
5	An arc on a unit circle has length 2π units. Find the central angle in radians.	2π radians
6	The minor arc subtended by a central angle on a unit circle has length $\pi/8$ units. Find the angle measure in radians.	$\pi/8$ radians

PART 2 • APPLY IT

- $13\pi/12$ radians** Because the dial is a unit circle, the arc length and radian measure are equal. The angle is $13\pi/12$ radians.
- $-5\pi/8$ units** On a unit circle, signed arc length equals the signed angle measure in radians. The clockwise motion gives a negative arc length of $-5\pi/8$ units.

CHALLENGE

Total angle measure: $19\pi/6$ radians. Coterminal angle: $7\pi/6$ radians, because $19\pi/6 - 2\pi = 19\pi/6 - 12\pi/6 = 7\pi/6$.

Accept equivalent fractions and equivalent forms of 2π . For signed arc lengths, accept a negative value only when the direction is stated as clockwise or otherwise negative.