

Volume Vault

Find exact volumes of familiar 3D solids.

HIGH SCHOOL • HSG-GMD.A.3

CCSS.Math.Content.HSG-GMD.A.3 "Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems. *"

NAME _____

DATE _____

VOLUME FORMULAS

Use $V = \pi r^2 h$ for a cylinder, $V = \frac{1}{3}\pi r^2 h$ for a cone, $V = \frac{1}{3}Bh$ for a pyramid, and $V = \frac{4}{3}\pi r^3$ for a sphere. In a pyramid formula, B is the area of the base. Keep π in your answer unless a decimal is requested.

WORKED EXAMPLE

Find the volume of a cylinder with radius 4 cm and height 7 cm.

1. $V = \pi r^2 h$
2. $V = \pi(4)^2(7)$
3. $V = 112\pi \text{ cm}^3$

Answer: $112\pi \text{ cm}^3$

PRACTICE 6 problems

- 1** Find the volume of a cylinder with radius 2 cm and height 9 cm.

ANSWER _____

- 2** Find the volume of a cone with radius 6 cm and height 12 cm.

ANSWER _____

- 3** Find the volume of a sphere with radius 3 cm.

ANSWER _____

- 4** Find the volume of a square pyramid with base side length 10 m and height 15 m.

ANSWER _____

- 5** Find the volume of a rectangular pyramid with a base that is 8 in. by 5 in. and a height of 6 in.

ANSWER _____

- 6** A cone has radius 9 cm and volume $162\pi \text{ cm}^3$. Find its height.

ANSWER _____

APPLY IT Show your work

- 1** A student designs a cylindrical water bottle with an inside radius of 6 cm and a height of 10 cm. What is the bottle's capacity in cubic centimeters, in terms of π ?

WORK SPACE

ANSWER _____

- 2** A school fundraiser serves shaved ice in cone-shaped cups with radius 6 cm and height 15 cm. What is the capacity of one cup, in terms of π ?

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

A model rocket has a cylindrical body with radius 6 cm and height 10 cm. Its nose is a cone with the same radius and a height of 9 cm. Find the total volume of the rocket, in terms of π .

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	Find the volume of a cylinder with radius 2 cm and height 9 cm.	$36\pi \text{ cm}^3$
2	Find the volume of a cone with radius 6 cm and height 12 cm.	$144\pi \text{ cm}^3$
3	Find the volume of a sphere with radius 3 cm.	$36\pi \text{ cm}^3$
4	Find the volume of a square pyramid with base side length 10 m and height 15 m.	500 m^3
5	Find the volume of a rectangular pyramid with a base that is 8 in. by 5 in. and a height of 6 in.	80 in.^3
6	A cone has radius 9 cm and volume $162\pi \text{ cm}^3$. Find its height.	6 cm

PART 2 • APPLY IT

- $360\pi \text{ cm}^3$** Use $V = \pi r^2 h$. Substitute 6 for r and 10 for h : $\pi(6)^2(10) = 360\pi \text{ cm}^3$.
- $180\pi \text{ cm}^3$** Use $V = \frac{1}{3}\pi r^2 h$. Substitute 6 for r and 15 for h : $\frac{1}{3}\pi(6)^2(15) = 180\pi \text{ cm}^3$.

CHALLENGE

 $468\pi \text{ cm}^3$

Accept equivalent exact forms that include π and correct cubic units. For the challenge, students should add the cylinder volume, $360\pi \text{ cm}^3$, and the cone volume, $108\pi \text{ cm}^3$.