

Triangle Signal Lab

Use sine and cosine rules to measure any triangle.

HIGH SCHOOL • HSG-SRT.D.11

CCSS.Math.Content.HSG-SRT.D.11 "(+) Understand and apply the Law of Sines and the Law of Cosines to find unknown measurements in right and non-right triangles (e.g., surveying problems, resultant forces)."

NAME _____

DATE _____

CHOOSE THE RIGHT RULE

Use the Law of Cosines when you know two sides and their included angle, or when you know all three sides: $c^2 = a^2 + b^2 - 2ab \cos C$. Use the Law of Sines when you know an angle and its opposite side: $a/\sin A = b/\sin B = c/\sin C$. Match each side with the angle directly across from it.

WORKED EXAMPLE

In a triangle, sides $a = 7$ and $b = 11$ include angle $C = 45^\circ$. Find c exactly.

$$1. c^2 = 7^2 + 11^2 - 2(7)(11)\cos 45^\circ$$

$$2. c^2 = 49 + 121 - 154(\sqrt{2}/2)$$

$$3. c^2 = 170 - 77\sqrt{2}$$

$$4. c = \sqrt{170 - 77\sqrt{2}}$$

Answer: $c = \sqrt{170 - 77\sqrt{2}}$

PRACTICE 6 problems

- 1** Sides $a = 6$ and $b = 8$ include angle $C = 60^\circ$. Find c exactly.

ANSWER _____

- 2** Two sides of a triangle are 10 and 10, and the included angle is 120° . Find the third side exactly.

ANSWER _____

- 3** In triangle ABC, $A = 30^\circ$, $a = 9$, and $B = 90^\circ$. Find b .

ANSWER _____

- 4** In triangle ABC, $A = 60^\circ$, $a = 6\sqrt{3}$, and $B = 30^\circ$. Find b .

ANSWER _____

- 5** A triangle has side lengths 13, 15, and 17. Let C be the angle opposite the side of length 17. Find $\cos C$.

ANSWER _____

- 6** In triangle ABC, $A = 30^\circ$, $a = 12$, and $B = 60^\circ$. Find b exactly.

ANSWER _____

APPLY IT Show your work

- 1** An environmental club maps two trail markers, P and Q, from a water station B. Marker P is 18 m from B, marker Q is 24 m from B, and angle PBQ is 60° . How far apart are P and Q? Give an exact answer.

WORK SPACE

ANSWER _____

- 2** A student videographer uses two marked spots A and B to frame a soccer goal at C. Triangle ABC has angle $A = 30^\circ$, angle $B = 60^\circ$, and $AB = 20$ m. Find AC exactly.

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

In triangle ABC, $A = 30^\circ$, $a = 5$, and $b = 5\sqrt{3}$. How many different triangles are possible? Give the possible values of C and c. Explain briefly.

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	Sides $a = 6$ and $b = 8$ include angle $C = 60^\circ$. Find c exactly.	$c = 2\sqrt{13}$
2	Two sides of a triangle are 10 and 10, and the included angle is 120° . Find the third side exactly.	$10\sqrt{3}$
3	In triangle ABC, $A = 30^\circ$, $a = 9$, and $B = 90^\circ$. Find b .	$b = 18$
4	In triangle ABC, $A = 60^\circ$, $a = 6\sqrt{3}$, and $B = 30^\circ$. Find b .	$b = 6$
5	A triangle has side lengths 13, 15, and 17. Let C be the angle opposite the side of length 17. Find $\cos C$.	$\cos C = 7/26$
6	In triangle ABC, $A = 30^\circ$, $a = 12$, and $B = 60^\circ$. Find b exactly.	$b = 12\sqrt{3}$

PART 2 • APPLY IT

- PQ = $6\sqrt{13}$ m** Use the Law of Cosines with the two distances and their included 60° angle. $PQ^2 = 18^2 + 24^2 - 2(18)(24)\cos 60^\circ = 468$, so $PQ = 6\sqrt{13}$ m.
- AC = $10\sqrt{3}$ m** First, angle $C = 90^\circ$, so AB is opposite 90° . Apply the Law of Sines: $AC/\sin 60^\circ = 20/\sin 90^\circ$, giving $AC = 10\sqrt{3}$ m.

CHALLENGE

Two triangles are possible: $(C, c) = (90^\circ, 10)$ or $(30^\circ, 5)$. Since $\sin B = (b \sin A)/a = \sqrt{3}/2$, B can be 60° or 120° .

Accept equivalent exact radical forms and correctly simplified unsimplified radical forms. For the challenge, accept either order of the two possible triangles if both are given with a valid sine-based explanation.