

Imaginary Root Quest

Solve quadratic equations with nonreal roots.

HIGH SCHOOL • HSN-CN.C

CCSS.Math.Content.HSN-CN.C "Use complex numbers in polynomial identities and equations."

NAME _____

DATE _____

WHEN ROOTS ARE COMPLEX

For $ax^2 + bx + c = 0$, use the quadratic formula. If the discriminant, $b^2 - 4ac$, is negative, rewrite its square root using i , where $i^2 = -1$. The two solutions will be complex conjugates.

WORKED EXAMPLE

Solve $x^2 + 10x + 26 = 0$.

- Here $a = 1$, $b = 10$, and $c = 26$.
- $b^2 - 4ac = 10^2 - 4(1)(26) = -4$.
- $x = \frac{-10 \pm \sqrt{-4}}{2} = \frac{-10 \pm 2i}{2}$.

Answer: $x = -5 \pm i$

PRACTICE 6 problems

1 Solve $x^2 + 9 = 0$.

ANSWER _____

2 Solve $x^2 - 8x + 20 = 0$.

ANSWER _____

3 Solve $2x^2 + 6x + 18 = 0$.

ANSWER _____

4 Solve $x^2 + 14x + 58 = 0$.

ANSWER _____

5 Solve $3x^2 - 18x + 35 = 0$.

ANSWER _____

6 Solve $6x^2 + 6x + 11 = 0$.

ANSWER _____

APPLY IT Show your work

- 1** A student game designer uses $R(x) = x^2 - 12x + 40$ to model the number of bug reports predicted after x testing rounds. Solve $R(x) = 0$. What do the solutions mean in this context?

WORK SPACE

ANSWER _____

- 2** A photography club tests a phone camera focus model, $F(x) = 2x^2 + 8x + 17$, where x is a filter adjustment setting. Solve $F(x) = 0$. What do the solutions mean for real filter settings?

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

Solve $x^4 + 16 = 0$. List all four complex roots.

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	Solve $x^2 + 9 = 0$.	$x = \pm 3i$
2	Solve $x^2 - 8x + 20 = 0$.	$x = 4 \pm 2i$
3	Solve $2x^2 + 6x + 18 = 0$.	$x = \frac{-3 \pm 3\sqrt{3}i}{2}$
4	Solve $x^2 + 14x + 58 = 0$.	$x = -7 \pm 3i$
5	Solve $3x^2 - 18x + 35 = 0$.	$x = 3 \pm \frac{2\sqrt{6}}{3}i$
6	Solve $6x^2 + 6x + 11 = 0$.	$x = -\frac{1}{2} \pm \frac{\sqrt{57}}{6}i$

PART 2 • APPLY IT

- $x = 6 \pm 2i$. There is no real number of testing rounds for which the model predicts 0 bug reports.** Use the quadratic formula to get $x = \frac{(12 \pm \sqrt{12^2 - 4(1)(40)})}{2} = 6 \pm 2i$. Since testing rounds must be real, the model never reaches 0 bug reports.
- $x = -2 \pm \frac{3\sqrt{2}}{2}i$. No real filter setting makes $F(x)$ equal to 0.** The quadratic formula gives $x = \frac{-8 \pm \sqrt{8^2 - 4(2)(17)}}{4} = -2 \pm \frac{3\sqrt{2}}{2}i$. Because both roots are nonreal, there is no real adjustment setting with a focus rating of 0.

CHALLENGE

$x = \sqrt{2} + \sqrt{2}i, \sqrt{2} - \sqrt{2}i, -\sqrt{2} + \sqrt{2}i, \text{ or } -\sqrt{2} - \sqrt{2}i$

Accept equivalent complex-number forms and roots listed in any order. For the challenge, students must include all four distinct roots.