

Vector Motion Lab

Combine directions, speeds, and displacements with vectors.

HIGH SCHOOL • HSN-VM.A.3

CCSS.Math.Content.HSN-VM.A.3 "(+) Solve problems involving velocity and other quantities that can be represented by vectors."

NAME _____

DATE _____

COMBINE COMPONENTS

Add or subtract vectors by combining their matching horizontal and vertical components. To find the speed represented by $\langle a, b \rangle$, calculate $\sqrt{a^2 + b^2}$, then include the correct units.

WORKED EXAMPLE

Find the resultant of $\langle 31, -22 \rangle + \langle -13, 47 \rangle$.

1. Add the horizontal components: $31 + (-13) = 18$.
2. Add the vertical components: $-22 + 47 = 25$.
3. Write the resultant vector as $\langle 18, 25 \rangle$.

Answer: $\langle 18, 25 \rangle$

PRACTICE 6 problems

1 Find $\langle 2, -9 \rangle + \langle 7, 12 \rangle$.

ANSWER _____

2 Find $\langle 15, 3 \rangle - \langle -4, 10 \rangle$.

ANSWER _____

3 Find $3\langle -4, 7 \rangle$.

ANSWER _____

4 Find the magnitude of $\langle 12, -9 \rangle$.

ANSWER _____

5 A velocity vector is $\langle 0, -16 \rangle$ m/s. What is the object's speed?

ANSWER _____

6 Let $w = \langle 8, 2 \rangle$. Find $2w$.

ANSWER _____

APPLY IT Show your work

- 1** At a robotics competition, a robot moves $\langle 14, 11 \rangle$ feet during its first command and then moves $\langle -6, 9 \rangle$ feet during its second command. What is the robot's net displacement vector?

WORK SPACE

ANSWER _____

- 2** A teen kayaker paddles with a velocity of $\langle 9, 4 \rangle$ mph relative to the water. The river current has velocity $\langle -3, 2 \rangle$ mph. What is the kayaker's ground velocity and ground speed?

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

A rescue drone needs a ground velocity of $\langle 16, -11 \rangle$ m/s. Wind adds a velocity of $\langle -4, 5 \rangle$ m/s to the drone's motion. What velocity must the drone have relative to the air? Then find its airspeed.

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	Find $\langle 2, -9 \rangle + \langle 7, 12 \rangle$.	$\langle 9, 3 \rangle$
2	Find $\langle 15, 3 \rangle - \langle -4, 10 \rangle$.	$\langle 19, -7 \rangle$
3	Find $3\langle -4, 7 \rangle$.	$\langle -12, 21 \rangle$
4	Find the magnitude of $\langle 12, -9 \rangle$.	15
5	A velocity vector is $\langle 0, -16 \rangle$ m/s. What is the object's speed?	16 m/s
6	Let $w = \langle 8, 2 \rangle$. Find $2w$.	$\langle 16, 4 \rangle$

PART 2 • APPLY IT

- $\langle 8, 20 \rangle$ feet** Add corresponding components: $\langle 14 + (-6), 11 + 9 \rangle = \langle 8, 20 \rangle$. The positive components show an eastward and northward net displacement.
- Ground velocity: $\langle 6, 6 \rangle$ mph; ground speed: $6\sqrt{2}$ mph** Add the paddling velocity and current: $\langle 9 + (-3), 4 + 2 \rangle = \langle 6, 6 \rangle$. The speed is $\sqrt{6^2 + 6^2} = \sqrt{72} = 6\sqrt{2}$ mph.

CHALLENGE

Velocity relative to the air: $\langle 20, -16 \rangle$ m/s; airspeed: $4\sqrt{41}$ m/s

Accept equivalent vector notation, such as $(9, 3)$, when the component order is clear. Accept $\sqrt{72}$ for the kayaker's speed and $\sqrt{656}$ for the drone's airspeed, although simplified radicals are preferred.