

Vector Scale Lab

Multiply components, then track direction and length.

HIGH SCHOOL • HSN-VM.B.5a

CCSS.Math.Content.HSN-VM.B.5a "Represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise, e.g., as $c(v_x, v_y) = (cv_x, cv_y)$."

NAME _____

DATE _____

SCALE A VECTOR

To multiply a vector by a scalar, multiply each component by that scalar. A positive scalar keeps the direction, while a negative scalar reverses it. The scalar's absolute value tells how the vector's length changes.

WORKED EXAMPLE

Find $7(-3, 5)$.

1. Multiply the x-component: $7 \times -3 = -21$.
2. Multiply the y-component: $7 \times 5 = 35$.
3. Write the new vector: $(-21, 35)$.

Answer: $7(-3, 5) = (-21, 35)$. The direction stays the same, and the length is 7 times as large.

PRACTICE 6 problems

1 Find $4(2, -6)$.

ANSWER _____

2 Find $-2(-4, 9)$.

ANSWER _____

3 Find $\frac{1}{2}(12, -8)$.

ANSWER _____

4 Let $a = (10, -1)$. Find $-a$. State whether the direction reverses.

ANSWER _____

5 Let $u = (-2, 11)$. Find $-4u$.

ANSWER _____

6 A vector has components $(8, 4)$. Multiply it by $-\frac{1}{2}$. State the direction and length change.

ANSWER _____

APPLY IT Show your work

- 1** A robotics team programs a rover to move along vector $r = (4, -6)$ meters. For a longer test, the team programs the rover to use $2r$. What is the new movement vector? Describe its direction and length.

WORK SPACE

ANSWER _____

- 2** In a video game, a character's knockback vector is $(12, -8)$. A power-up applies $-1/2$ times this vector. What is the new knockback vector? Describe the change in direction and distance.

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

A vector v satisfies $-2v = (8, -12)$. Find v . Explain what multiplying v by -2 did to v .

PART 1 · PRACTICE

#	PROBLEM	ANSWER
1	Find $4(2, -6)$.	(8, -24)
2	Find $-2(-4, 9)$.	(8, -18)
3	Find $\frac{1}{2}(12, -8)$.	(6, -4)
4	Let $a = (10, -1)$. Find $-a$. State whether the direction reverses.	$-a = (-10, 1)$; the direction reverses.
5	Let $u = (-2, 11)$. Find $-4u$.	(8, -44)
6	A vector has components (8, 4). Multiply it by $-1/2$. State the direction and length change.	(-4, -2); the direction reverses, and the length is half as long.

PART 2 · APPLY IT

- $2r = (8, -12)$ meters. The rover moves in the same direction, twice as far.** Multiply both components of (4, -6) by 2. Because the scalar is positive, the direction stays the same.
- $(-6, 4)$. The knockback reverses direction and travels half the distance.** Multiply each component by $-1/2$. The negative scalar reverses direction, and an absolute value of $1/2$ halves the length.

CHALLENGE

$v = (-4, 6)$. Multiplying v by -2 reversed its direction and doubled its length.

Accept equivalent vector notation, such as $\langle 8, -24 \rangle$ in place of (8, -24). For direction descriptions, accept "opposite direction" for "reverses direction," and "twice the length" for "doubles its length."