

Prism Power

Use a layer model and a formula to find volume.

GRADE 6 • MA.6.GR.2.3

MA.6.GR.2.3 "Solve mathematical and real-world problems involving the volume of right rectangular prisms with positive rational number edge lengths using a visual model and a formula."

NAME _____

DATE _____

BUILD VOLUME WITH LAYERS

A right rectangular prism is made of equal-sized layers.
Multiply length $\times$ width $\times$ height to find volume: $V = l \times w \times h$. A layer or array model shows the rows and columns of the base, and the height tells how tall the layers are.

WORKED EXAMPLE

Find the volume of a right rectangular prism with length 3 units, width 2 units, and height $1\frac{1}{2}$ unit.

1. Visual model, one layer that is $1\frac{1}{2}$ unit tall. Each box has a 1 unit by 1 unit base: $+---+---+---+ ||| +---+---+---+ |||$
 $+---+---+---+ 3$ columns, 2 rows
2. The base has $3 \times 2 = 6$ square units.
3. Use $V = l \times w \times h = 3 \times 2 \times 1\frac{1}{2}$.
4. Multiply: $6 \times 1\frac{1}{2} = 3$ cubic units.

Answer: 3 cubic units

PRACTICE 6 problems

- 1** PRACTICE 1. Find the volume of a right rectangular prism with length 4 units, width 5 units, and height $1\frac{1}{4}$ unit.

ANSWER _____

- 2** 2. Find the volume of a right rectangular prism with length $7\frac{1}{4}$ unit, width $8\frac{1}{5}$ unit, and height $5\frac{1}{7}$ unit.

ANSWER _____

- 3** 3. Find the volume of a right rectangular prism with length $9\frac{1}{10}$ unit, width $4\frac{1}{9}$ unit, and height $5\frac{1}{8}$ unit.

ANSWER _____

- 4** 4. Find the volume of a right rectangular prism with length $11\frac{1}{6}$ units, width $12\frac{1}{11}$ units, and height $5\frac{1}{12}$ unit.

ANSWER _____

- 5** 5. Find the volume of a right rectangular prism with length $7\frac{1}{8}$ unit, width $16\frac{1}{7}$ units, and height $15\frac{1}{16}$ unit.

ANSWER _____

- 6** 6. A right rectangular prism has a volume of $35\frac{1}{12}$ cubic units. Its length is $7\frac{1}{6}$ units and its width is $5\frac{1}{4}$ units. Find its height.

ANSWER _____

APPLY IT Show your work

- 1** APPLY 1. A school gaming club stores controllers in a rectangular clear bin. The bin is $\frac{5}{4}$ feet long, $\frac{7}{6}$ feet wide, and $\frac{12}{5}$ feet high. What is the volume of the bin?

WORK SPACE

ANSWER _____

- 2** 2. Students are building a rectangular planter for a pollinator garden. The planter is $\frac{15}{8}$ feet long, $\frac{4}{5}$ foot wide, and $\frac{14}{9}$ foot high. What is the volume of the planter?

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

CHALLENGE Maya says that a right rectangular prism with length $\frac{5}{6}$ unit, width $\frac{9}{5}$ unit, and height $\frac{8}{9}$ unit has a volume of $\frac{8}{3}$ cubic units. Is Maya correct? Explain using the volume formula.

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	PRACTICE 1. Find the volume of a right rectangular prism with length 4 units, width 5 units, and height $\frac{1}{4}$ unit.	5 cubic units
2	2. Find the volume of a right rectangular prism with length $\frac{7}{4}$ unit, width $\frac{8}{5}$ unit, and height $\frac{5}{7}$ unit.	2 cubic units
3	3. Find the volume of a right rectangular prism with length $\frac{9}{10}$ unit, width $\frac{4}{9}$ unit, and height $\frac{5}{8}$ unit.	$\frac{1}{4}$ cubic unit
4	4. Find the volume of a right rectangular prism with length $\frac{11}{6}$ units, width $\frac{12}{11}$ units, and height $\frac{5}{12}$ unit.	$\frac{5}{6}$ cubic unit
5	5. Find the volume of a right rectangular prism with length $\frac{7}{8}$ unit, width $\frac{16}{7}$ units, and height $\frac{15}{16}$ unit.	$\frac{15}{8}$ cubic units
6	6. A right rectangular prism has a volume of $\frac{35}{12}$ cubic units. Its length is $\frac{7}{6}$ units and its width is $\frac{5}{4}$ units. Find its height.	2 units

PART 2 • APPLY IT

- $\frac{7}{2}$ cubic feet** Use $V = l \times w \times h$. $(\frac{5}{4}) \times (\frac{7}{6}) \times (\frac{12}{5}) = \frac{7}{2}$.
- $\frac{7}{3}$ cubic feet** Use $V = l \times w \times h$. $(\frac{15}{8}) \times (\frac{4}{5}) \times (\frac{14}{9}) = \frac{7}{3}$.

CHALLENGE

No. $V = (\frac{5}{6}) \times (\frac{9}{5}) \times (\frac{8}{9}) = \frac{4}{3}$ cubic units, not $\frac{8}{3}$ cubic units.

Accept equivalent fraction forms, such as $1 \frac{1}{2}$ cubic units for $\frac{3}{2}$ cubic units. Require cubic units for volume answers and units for the missing height.