

Exponent Power Quest

Use integer exponents to simplify rational-number powers.

GRADE 8 • MA.8.NSO.1.3

MA.8.NSO.1.3 "Extend previous understanding of the Laws of Exponents to include integer exponents. Apply the Laws of Exponents to evaluate numerical expressions and generate equivalent numerical expressions..."

NAME _____

DATE _____

THE BIG IDEA

For any nonzero rational number a , $a^{-n} = 1/a^n$ and $a^0 = 1$. When multiplying powers with the same base, add exponents, and when dividing, subtract exponents before evaluating.

WORKED EXAMPLE

Evaluate: $(7/11)^{-4} * (7/11)^5$

1. Add the exponents: $-4 + 5 = 1$.
2. $(7/11)^{-4} * (7/11)^5 = (7/11)^1$.
3. Evaluate the power: $(7/11)^1 = 7/11$.

Answer: 7/11

PRACTICE 6 problems

1 Evaluate: $(3/10)^{-2}$

ANSWER _____

2 Evaluate: $(-1/2)^3$

ANSWER _____

3 Write as one power, then evaluate: $(6/13)^2 * (6/13)^{-3}$

ANSWER _____

4 Evaluate: $(-2/9)^{-3}$

ANSWER _____

5 Evaluate: $(9/2)^0$

ANSWER _____

6 Simplify, then evaluate: $(2/3)^3 / (2/3)^{-2}$

ANSWER _____

APPLY IT Show your work

- 1** A streamer compresses a video before posting it. Each processing pass keeps $\frac{2}{3}$ of the video's current file size. What fraction of the original file size remains after 3 passes?

WORK SPACE

ANSWER _____

- 2** A student shrinks a poster image so its area becomes $(\frac{2}{3})^3$ of the original area. What factor must multiply the smaller area to restore the original area? Write and evaluate the factor as $(\frac{2}{3})^{-3}$.

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

Simplify and evaluate. Explain how you combined the exponents: $[(-\frac{2}{3})^{-2} * (-\frac{2}{3})^3] / (-\frac{2}{3})^2$

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	Evaluate: $(3/10)^{-2}$	100/9
2	Evaluate: $(-1/2)^3$	-1/8
3	Write as one power, then evaluate: $(6/13)^2 \cdot (6/13)^{-3}$	13/6
4	Evaluate: $(-2/9)^{-3}$	-729/8
5	Evaluate: $(9/2)^0$	1
6	Simplify, then evaluate: $(2/3)^3 \div (2/3)^{-2}$	32/243

PART 2 • APPLY IT

- 8/27 of the original file size** Multiply the same factor three times: $(2/3)^3 = 8/27$. The final file is 8/27 of the original size.
- 27/8** A negative exponent means use the reciprocal: $(2/3)^{-3} = (3/2)^3 = 27/8$.

CHALLENGE

-3/2. The exponents combine to $-2 + 3 - 2 = -1$, so the expression is $(-2/3)^{-1} = -3/2$.

Accept equivalent reciprocal power forms in student work, such as $(10/3)^2$ for problem 1, but final evaluated fractions should be simplified. For the challenge, accept any correct explanation that adds exponents when multiplying and subtracts the divisor's exponent.