

# Divide and Conquer

*Simplify polynomial quotients one term at a time.*

**HIGH SCHOOL • MA.912.AR.1.4**

**MA.912.AR.1.4** "Divide a polynomial expression by a monomial expression with rational number coefficients."

NAME \_\_\_\_\_

DATE \_\_\_\_\_

## DIVIDE EVERY TERM

Divide each term in the polynomial by the monomial. Divide the coefficients, then subtract the exponent of  $x$  in the divisor from each exponent of  $x$  in the dividend. When dividing by a fraction, multiply by its reciprocal.

## WORKED EXAMPLE

$$(34x^5 - 51x^4 + 68x^3) / (17x)$$

$$1. (34/17)x^{(5-1)} - (51/17)x^{(4-1)} + (68/17)x^{(3-1)}$$

$$2. = 2x^4 - 3x^3 + 4x^2$$

3. Each term is divided by  $17x$ .

**Answer:  $2x^4 - 3x^3 + 4x^2$**

## PRACTICE 6 problems

**1**  $(35x^4 - 49x^3) / (7x)$

ANSWER \_\_\_\_\_

**2**  $(-44x^5 + 22x^3) / (-11x)$

ANSWER \_\_\_\_\_

**3**  $((10/9)x^6 - (25/18)x^5) / ((5/18)x)$

ANSWER \_\_\_\_\_

**4**  $((-33/7)x^7 + (55/7)x^6) / ((11/14)x)$

ANSWER \_\_\_\_\_

**5**  $(63x^8 + 27x^7 - 45x^6) / (-9x^2)$

ANSWER \_\_\_\_\_

**6**  $((45/14)x^9 - (15/7)x^8) / (-(5/14)x^3)$

ANSWER \_\_\_\_\_

## APPLY IT Show your work

- 1** An esports club models its total prize fund as  $(\frac{21}{4})x^3 + (\frac{7}{2})x^2$  dollars. The club assigns  $(\frac{7}{4})x$  equal prize shares. Write a simplified expression for the dollars in each prize share.

WORK SPACE

ANSWER \_\_\_\_\_

- 2** A student film crew models its total editing time as  $(\frac{15}{11})x^4 - (\frac{10}{11})x^3 + (\frac{25}{11})x^2$  minutes. The work is split equally among  $(\frac{5}{11})x$  editing stations. Write a simplified expression for the minutes of work at each station.

WORK SPACE

ANSWER \_\_\_\_\_

## CHALLENGE One step up

### CHALLENGE

Divide, then explain why the quotient has no  $x^5$  term:  $((\frac{7}{9})x^8 - (\frac{14}{27})x^6 + (\frac{35}{18})x^5) / (-\frac{7}{18}x^2)$ .

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## PART 1 · PRACTICE

| # | PROBLEM                                   | ANSWER                |
|---|-------------------------------------------|-----------------------|
| 1 | $(35x^4 - 49x^3) / (7x)$                  | $5x^3 - 7x^2$         |
| 2 | $(-44x^5 + 22x^3) / (-11x)$               | $4x^4 - 2x^2$         |
| 3 | $((10/9)x^6 - (25/18)x^5) / ((5/18)x)$    | $4x^5 - 5x^4$         |
| 4 | $((-33/7)x^7 + (55/7)x^6) / ((11/14)x)$   | $-6x^6 + 10x^5$       |
| 5 | $(63x^8 + 27x^7 - 45x^6) / (-9x^2)$       | $-7x^6 - 3x^5 + 5x^4$ |
| 6 | $((45/14)x^9 - (15/7)x^8) / (-(5/14)x^3)$ | $-9x^6 + 6x^5$        |

## PART 2 · APPLY IT

- $3x^2 + 2x$  dollars per prize share** Divide each term of the prize-fund expression by  $(7/4)x$ . The quotient is  $3x^2 + 2x$ .
- $3x^3 - 2x^2 + 5x$  minutes per editing station** Divide each term of the total-time expression by  $(5/11)x$ . The quotient is  $3x^3 - 2x^2 + 5x$ .

## CHALLENGE

**$-2x^6 + (4/3)x^4 - 5x^3$ . The quotient has no  $x^5$  term because the dividend has no  $x^7$  term.**

Accept equivalent simplified quotients with terms in any order. Require students to divide every term and reduce rational coefficients.