

Remainder Reveal

Use polynomial values to find remainders quickly.

HIGH SCHOOL • MA.912.AR.6.2

MA.912.AR.6.2 "Explain and apply the Remainder Theorem to solve mathematical and real-world problems."

NAME _____

DATE _____

THE BIG IDEA

When $P(x)$ is divided by $x-a$, the remainder is $P(a)$. To find the remainder, substitute a into the polynomial and simplify.

WORKED EXAMPLE

Find the remainder when $P(x)=23x-29$ is divided by $x-8$.

1. The divisor $x-8$ has a value of 8.
2. Find $P(8)$.
3. $P(8)=23(8)-29=184-29=155$.

Answer: 155

PRACTICE 6 problems

- 1** Find the remainder when $P(x)=x^2+3x-5$ is divided by $x-2$.

ANSWER _____

- 2** Find the remainder when $P(x)=x^3-6x+1$ is divided by $x+1$.

ANSWER _____

- 3** Find the remainder when $P(x)=2x^2-9x+7$ is divided by $x-5$.

ANSWER _____

- 4** Find k if $P(x)=x^2+kx+10$ has a remainder of 1 when divided by $x-3$.

ANSWER _____

- 5** Find the remainder when $P(x)=x^3-2x^2+5$ is divided by $x-2$.

ANSWER _____

- 6** Find the remainder when $P(x)=3x^2+x-12$ is divided by $x+6$.

ANSWER _____

APPLY IT Show your work

- 1** A pop-up shop models its daily profit, in dollars, by $E(x)=x^3-6x+10$, where x is the number of dozens of shirts sold. Use the Remainder Theorem to find the predicted profit when 5 dozen shirts are sold.

WORK SPACE

ANSWER _____

- 2** A robotics club models its net profit, in tens of dollars, by $P(x)=2x^3-3x^2-9x+10$, where x is the number of ticket bundles sold. Use the Remainder Theorem to find the net profit when 2 ticket bundles are sold.

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

The polynomial $P(x)=x^3+ax^2+bx-6$ has a remainder of 0 when divided by $x-2$ and also when divided by $x+1$. Find a and b .

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	Find the remainder when $P(x)=x^2+3x-5$ is divided by $x-2$.	5
2	Find the remainder when $P(x)=x^3-6x+1$ is divided by $x+1$.	6
3	Find the remainder when $P(x)=2x^2-9x+7$ is divided by $x-5$.	12
4	Find k if $P(x)=x^2+kx+10$ has a remainder of 1 when divided by $x-3$.	$k=-6$
5	Find the remainder when $P(x)=x^3-2x^2+5$ is divided by $x-2$.	5
6	Find the remainder when $P(x)=3x^2+x-12$ is divided by $x+6$.	90

PART 2 • APPLY IT

1. **\$105** Evaluate $E(5)$, which is the remainder when $E(x)$ is divided by $x-5$. $E(5)=125-30+10=105$.
2. **-\$40, meaning a loss of \$40** Evaluate $P(2)$, which is the remainder when $P(x)$ is divided by $x-2$. $P(2)=-4$, and -4 tens of dollars is -\$40.

CHALLENGE

$a=2, b=-5$

Accept correct substitution work using $P(a)$, including equivalent arithmetic expressions. For the challenge, accept equations $P(2)=0$ and $P(-1)=0$ followed by $a=2$ and $b=-5$.