

Factor, Solve, Sketch

Use zeros and multiplicity to graph polynomials.

HIGH SCHOOL • MA.912.AR.6.6

MA.912.AR.6.6 "Solve and graph mathematical and real-world problems that are modeled with polynomial functions of degree 3 or higher. Interpret key features and determine constraints in terms of the context."

NAME _____

DATE _____

ZEROS SHOW THE GRAPH

Set each factor equal to zero to find the zeros. A factor used once usually crosses the x-axis. An even-power factor touches the x-axis and turns around.

WORKED EXAMPLE

Sketch $y=(x-7)(x+3)(x-4)$.

1. Set each factor equal to zero.
2. $x-7=0$, $x+3=0$, and $x-4=0$.
3. The zeros are 7, -3, and 4. Each has multiplicity 1, so the graph crosses at each zero.

**Answer: x-intercepts: (7,0), (-3,0), (4,0).
Left end down, right end up.**

PRACTICE 5 problems

1 Solve $(x+5)(x-2)(x+1)=0$.

ANSWER _____

2 Solve $x(x-10)(x+2)=0$.

ANSWER _____

3 Sketch $y=(x+6)^2(x-9)$. State the x-intercepts and end behavior.

ANSWER _____

4 Sketch $y=-(x-10)(x+2)(x-5)(x+1)$. State the x-intercepts and end behavior.

ANSWER _____

5 Sketch $y=(x-11)^2(x+8)$. State the x-intercepts and end behavior.

ANSWER _____

APPLY IT Show your work

- 1** A drone club models a launched drone's height, in meters, by $h(t) = -t(t-6)(t+2)$, where t is time in seconds. When is the drone on the ground? Give the meaningful time domain.

WORK SPACE

ANSWER _____

- 2** A concert team models its profit by $P(x) = -(x-5)(x-12)(x+2)$, where x is the number of tickets sold in hundreds and $0 \leq x \leq 15$. Find the break-even sales and when profit is positive.

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

Without graphing every point, describe the key features of $y = -(x+9)(x-2)^2(x-6)$. Explain how multiplicity and degree determine the graph.

PART 1 · PRACTICE

#	PROBLEM	ANSWER
1	Solve $(x+5)(x-2)(x+1)=0$.	$x=-5, 2, -1$
2	Solve $x(x-10)(x+2)=0$.	$x=0, 10, -2$
3	Sketch $y=(x+6)^2(x-9)$. State the x-intercepts and end behavior.	x-intercepts: $(-6,0)$, where the graph touches, and $(9,0)$, where it crosses. Left end down, right end up.
4	Sketch $y=-(x-10)(x+2)(x-5)(x+1)$. State the x-intercepts and end behavior.	x-intercepts: $(-2,0)$, $(-1,0)$, $(5,0)$, $(10,0)$. The graph crosses at each intercept. Both ends down.
5	Sketch $y=(x-11)^2(x+8)$. State the x-intercepts and end behavior.	x-intercepts: $(-8,0)$, where the graph crosses, and $(11,0)$, where it touches. Left end down, right end up.

PART 2 · APPLY IT

- The drone is on the ground at $t=0$ and $t=6$. Meaningful domain: $0 \leq t \leq 6$.** Set each factor equal to zero to get $t=0, 6$, and -2 . Negative time is not meaningful, so use times from launch until landing.
- Break-even sales: 500 tickets and 1200 tickets. Profit is positive when $500 < x < 1200$ tickets.** The meaningful zeros are $x=5$ and $x=12$, since $x=-2$ is outside the context. Testing a value between the zeros shows $P(x)$ is positive there.

CHALLENGE

The x-intercepts are $(-9,0)$, $(2,0)$, and $(6,0)$. The graph crosses at -9 and 6 , touches and turns at 2 , and both ends point down because the polynomial has even degree with a negative leading coefficient.

Accept zeros in any order and equivalent interval notation. For sketches, accept any graph with the stated intercept behavior and end behavior.