

Confidence Check

Read margins of error with meaning.

HIGH SCHOOL • MA.912.DP.1.5

MA.912.DP.1.5 "Interpret the margin of error of a mean or percentage from a data set. Interpret the confidence level corresponding to the margin of error."

NAME _____

DATE _____

READ THE RANGE

A result of $p\% \pm m\%$ estimates the population percentage from $p - m\%$ to $p + m\%$. A mean uses the same rule in its own units. At a stated confidence level, the sampling method would produce intervals containing the true value about that percent of the time.

WORKED EXAMPLE

A random sample has a mean commute time of 52 minutes with a margin of error of 4 minutes at 90% confidence. Interpret the result.

1. Start with 52 minutes.
2. Lower end: $52 - 4 = 48$.
3. Upper end: $52 + 4 = 56$.
4. Use the stated confidence level.

Answer: The population mean is estimated to be 48 to 56 minutes. We are 90% confident that this interval contains the population mean.

PRACTICE 5 problems

- 1** A poll estimates 64% with a margin of error of 3 percentage points. Write the interval.

ANSWER _____

- 2** A sample mean is 18 books with a margin of error of 2 books. Interpret the estimate.

ANSWER _____

- 3** At 95% confidence, an estimate is 71% $\pm$ 5%. What does 95% confidence mean?

ANSWER _____

- 4** A report gives 39% $\pm$ 6%. Can the population percentage be 47% based on this estimate?

ANSWER _____

- 5** Survey A is 82% $\pm$ 2%. Survey B is 82% $\pm$ 7%. Which estimate is more precise?

ANSWER _____

APPLY IT Show your work

- 1** Student council surveys 120 randomly selected students. It finds that 58% want a later start time, with a margin of error of 5 percentage points at 95% confidence. Write and interpret the interval.

WORK SPACE

ANSWER _____

- 2** A health class randomly samples 25 students and finds a mean of 7.5 hours of sleep per night, with a margin of error of 0.5 hour at 80% confidence. Write and interpret the interval.

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

Two random polls at 95% confidence estimate support for a school club. Poll A is 46% $\pm$ 3%, and Poll B is 51% $\pm$ 3%. Do the intervals overlap? What can you conclude?

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	A poll estimates 64% with a margin of error of 3 percentage points. Write the interval.	61% to 67%
2	A sample mean is 18 books with a margin of error of 2 books. Interpret the estimate.	The population mean is estimated to be 16 to 20 books.
3	At 95% confidence, an estimate is 71% $\pm$ 5%. What does 95% confidence mean?	In repeated random samples using this method, about 95% of the intervals would contain the true population percentage.
4	A report gives 39% $\pm$ 6%. Can the population percentage be 47% based on this estimate?	No. The interval is 33% to 45%.
5	Survey A is 82% $\pm$ 2%. Survey B is 82% $\pm$ 7%. Which estimate is more precise?	Survey A, because it has the smaller margin of error.

PART 2 • APPLY IT

- 53% to 63%. We are 95% confident that the population percentage who want a later start time is in this interval.**
Subtract and add 5 to 58. Interpret 95% confidence as describing the reliability of the sampling method.
- 7 to 8 hours. We are 80% confident that the population mean sleep time is in this interval.** Subtract and add 0.5 to 7.5.
The interval estimates the population mean, not every student's sleep time.

CHALLENGE

Poll A: 43% to 49%. Poll B: 48% to 54%. The intervals overlap from 48% to 49%, so these estimates alone do not clearly show which population support percentage is higher.

Accept interval notation, such as [61%, 67%], when endpoints are correct. Confidence explanations should describe repeated random samples or intervals, not claim that 95% of individuals are in the interval.