

Function Face-Off

Compare linear functions by their rates, starting values, and outputs.

HIGH SCHOOL • MA.912.F.1

MA.912.F.1 "Understand, compare and analyze properties of functions."

NAME _____

DATE _____

PRACTICE: COMPARE LINEAR FUNCTIONS

For a linear function $y=mx+b$, m tells how much the output changes when x increases by 1, and b is the output when $x=0$. To compare linear functions, find each rate and initial value, then evaluate the functions at the requested input when needed.

WORKED EXAMPLE

For $y=11x+17$, identify the rate of change and initial value.

1. Write the rule in $y=mx+b$ form.
2. Match m with 11.
3. Match b with 17.

Answer: Rate of change: 11; initial value: 17.

PRACTICE 6 problems

- 1** For $f(x)=-3x+5$, state the rate of change and the initial value.

ANSWER _____

- 2** Function g is shown in the table. x : 0, 2, 4. $g(x)$: 1, 7, 13. Find the rate of change and initial value.

ANSWER _____

- 3** $p(x)=2x-4$. Function q is shown in the table. x : 0, 3, 6. $q(x)$: 2, 8, 14. Which function has the greater initial value? Do the functions have the same rate of change?

ANSWER _____

- 4** $a(x)=5x+1$ and $b(x)=3x+9$. Find the input where the functions have the same output. Then find that output.

ANSWER _____

- 5** A linear function passes through (2,-1) and (6,7). Write its equation in the form $y=mx+b$.

ANSWER _____

- 6** $r(x)=-4x+6$. Function s is shown in the table. x : -2, 0, 2. $s(x)$: 9, 3, -3. Which function has the greater value when $x=-2$, and by how much?

ANSWER _____

APPLY IT Show your work

- 1** APPLY 1: Two esports clubs charge total dues based on the number of months m . Club A charges $A(m)=4m+12$ dollars. Club B charges $B(m)=6m+2$ dollars. After how many months will the total costs be equal? What will each total cost be?

WORK SPACE

ANSWER _____

- 2** APPLY 2: Jay saves for a school trip using $J(t)=8t+24$, where t is weeks. Kai's savings are shown in the table. t : 0, 1, 2. $K(t)$: 40, 46, 52. Who has more money after 3 weeks? When will their savings be equal?

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

CHALLENGE: $h(x)=x^2-6x+8$ and $k(x)=2x-4$. For which integer values of x from 0 through 8 is $h(x)$ greater than $k(x)$? Explain your reasoning.

PART 1 · PRACTICE

#	PROBLEM	ANSWER
1	For $f(x) = -3x + 5$, state the rate of change and the initial value.	Rate of change: -3; initial value: 5.
2	Function g is shown in the table. x : 0, 2, 4. $g(x)$: 1, 7, 13. Find the rate of change and initial value.	Rate of change: 3; initial value: 1.
3	$p(x) = 2x - 4$. Function q is shown in the table. x : 0, 3, 6. $q(x)$: 2, 8, 14. Which function has the greater initial value? Do the functions have the same rate of change?	q has the greater initial value. Yes, both rates of change are 2.
4	$a(x) = 5x + 1$ and $b(x) = 3x + 9$. Find the input where the functions have the same output. Then find that output.	$x = 4$, and both outputs are 21.
5	A linear function passes through (2,-1) and (6,7). Write its equation in the form $y = mx + b$.	$y = 2x - 5$
6	$r(x) = -4x + 6$. Function s is shown in the table. x : -2, 0, 2. $s(x)$: 9, 3, -3. Which function has the greater value when $x = -2$, and by how much?	r has the greater value by 5.

PART 2 · APPLY IT

- After 5 months, each total cost is \$32.** Set $4m + 12$ equal to $6m + 2$ and solve to get $m = 5$. Substitute 5 into either function to get 32.
- After 3 weeks, Kai has \$58 and has \$10 more than Jay. Their savings will be equal after 8 weeks, when each has \$88.** Kai's table has a rate of 6 and an initial value of 40, so $K(t) = 6t + 40$. Compare both functions at $t = 3$, then solve $8t + 24 = 6t + 40$.

CHALLENGE

$x = 0, 1, 7$, and 8 . Since $h(x) - k(x) = x^2 - 8x + 12 = (x - 2)(x - 6)$, the difference is positive when $x < 2$ or $x > 6$. The stated integer values are $0, 1, 7$, and 8 .

Accept equivalent forms of the linear equation in problem 5. For comparison questions, accept correct values and conclusions supported by accurate rate, initial-value, or substitution work.