

Exponent Power Moves

Rewrite and simplify radicals and rational exponents.

HIGH SCHOOL • MA.912.NSO.1.3

MA.912.NSO.1.3 "Generate equivalent algebraic expressions involving radicals or rational exponents using the properties of exponents."

NAME _____

DATE _____

TWO WAYS TO WRITE A POWER

For a positive base, $a^{(m/n)}$ means take the n th root, then raise the result to the m th power. You can write $a^{(m/n)}$ as the n th root of a^m , or as $(\text{the } n\text{th root of } a)^m$. Use exponent rules to simplify after rewriting.

WORKED EXAMPLE

Simplify $625^{(3/4)}$.

1. $625 = 5^4$

2. $(5^4)^{(3/4)} = 5^3$

3. $5^3 = 125$

Answer: 125

PRACTICE 6 problems

- 1** For $x \geq 0$, rewrite the 4th root of x^7 using a rational exponent.

ANSWER _____

- 2** For $y \geq 0$, rewrite $y^{(5/6)}$ using a radical.

ANSWER _____

- 3** Simplify $64^{(5/6)}$.

ANSWER _____

- 4** Simplify the 3rd root of $216a^6$.

ANSWER _____

- 5** Rewrite $(\text{the } 5\text{th root of } b)^3$ using a rational exponent.

ANSWER _____

- 6** For $c \geq 0$, simplify $(16c^{12})^{(1/4)}$.

ANSWER _____

APPLY IT Show your work

- 1** A game designer makes a cube-shaped 3-D map tile with a volume of 2744 cubic meters. Its side length s satisfies $s^3 = 2744$. Write s using a rational exponent, then find the side length.

WORK SPACE

ANSWER _____

- 2** A student-made music app models an intensity setting with $I = p^4$. For one preset, $I = 1296$. Write the positive value of p using a radical, then find p .

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

For $x \geq 0$, simplify $(81x^{12})^{(3/4)}$. Show how the exponent $3/4$ affects both factors.

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	For $x \geq 0$, rewrite the 4th root of x^7 using a rational exponent.	$x^{(7/4)}$
2	For $y \geq 0$, rewrite $y^{(5/6)}$ using a radical.	6th root of y^5
3	Simplify $64^{(5/6)}$.	32
4	Simplify the 3rd root of $216a^6$.	$6a^2$
5	Rewrite (the 5th root of b) ³ using a rational exponent.	$b^{(3/5)}$
6	For $c \geq 0$, simplify $(16c^{12})^{(1/4)}$.	$2c^3$

PART 2 • APPLY IT

1. **$s = 2744^{(1/3)} = 14$ meters** Use the exponent $1/3$ to represent a cube root. Since $14^3 = 2744$, the side length is 14 meters.
2. **$p = 4\text{th root of } 1296 = 6$** Take the 4th root of both sides because p is raised to the 4th power. Since $6^4 = 1296$, $p = 6$.

CHALLENGE

$27x^9$

Accept equivalent radical forms, such as (6th root of y)⁵ for $y^{(5/6)}$. In the challenge, $81^{(3/4)} = 27$ and $(x^{12})^{(3/4)} = x^9$ under the stated condition.