

Transform and Track

Use coordinates to compare images and pre-images.

GRADE 8 • TEKS 8.10.A

8.10.A "generalize the properties of orientation and congruence of rotations, reflections, translations, and dilations of two-dimensional shapes on a coordinate plane;"

NAME _____

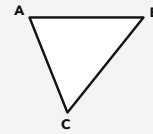
DATE _____

TRANSFORMATION PROPERTIES

Translations and rotations keep side lengths, angle measures, and orientation. Reflections keep lengths and angles but reverse orientation. A dilation multiplies all lengths by its scale factor, so it is congruent only when the scale factor is 1.

WORKED EXAMPLE

The triangle shown has $A(11,12)$, $B(14,12)$, and $C(12,15)$. Rotate it 90° counterclockwise about the origin. Find A' , B' , and C' .



1. Use the rule (x,y) to $(-y,x)$.
2. $A(11,12)$ becomes $A'(-12,11)$.
3. Apply the rule to B and C.

Answer: $A'(-12,11)$, $B'(-12,14)$, $C'(-15,12)$

PRACTICE 4 problems

- 1** Triangle DEF has $D(6,-3)$, $E(9,-3)$, and $F(7,-6)$. Reflect it across the y-axis. Give the image coordinates and state whether orientation changes.

ANSWER _____

- 2** Triangle MNP has $M(-4,7)$, $N(-1,7)$, and $P(-2,9)$. Translate it 5 units right and 8 units down. Is the image congruent to the pre-image?

ANSWER _____

- 3** Triangle QRS has $Q(8,10)$, $R(10,10)$, and $S(8,13)$. Dilate it by a scale factor of $1/2$ about the origin. Is the image congruent?

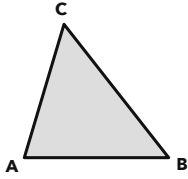
ANSWER _____

- 4** Triangle JKL has $J(-7,6)$, $K(-9,6)$, and $L(-8,8)$. Rotate it 180° about the origin. State whether orientation and congruence are preserved.

ANSWER _____

APPLY IT Show your work

- 1** A gaming club uses the shown triangle as a logo. Its vertices are $A(-2,3)$, $B(-5,3)$, and $C(-3,6)$. A screen effect reflects the logo across the y -axis. Find the new coordinates. Is the new logo congruent?



ANSWER _____

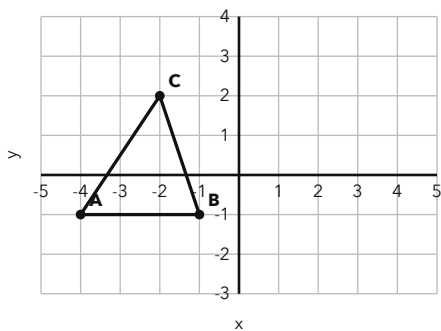
- 2** An animator enlarges a triangular sticker with vertices $U(2,-4)$, $V(4,-4)$, and $W(2,-2)$. The dilation has scale factor $3/2$ and center $(0,0)$. Find U' , V' , and W' . State whether orientation is preserved.

WORK SPACE

ANSWER _____

CHALLENGE One step up

The grid shows triangle ABC. Translate it 3 units right and 1 unit up, then reflect the result across the y -axis. Find A'' , B'' , and C'' . Is the final image congruent to triangle ABC, and is its orientation the same or reversed?



WORK SPACE AND ANSWER

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	Triangle DEF has D(6,-3), E(9,-3), and F(7,-6). Reflect it across the y-axis. Give the image coordinates and state whether orientation changes.	D'(-6,-3), E'(-9,-3), F'(-7,-6); orientation reverses.
2	Triangle MNP has M(-4,7), N(-1,7), and P(-2,9). Translate it 5 units right and 8 units down. Is the image congruent to the pre-image?	M'(1,-1), N'(4,-1), P'(3,1); yes, the image is congruent.
3	Triangle QRS has Q(8,10), R(10,10), and S(8,13). Dilate it by a scale factor of $\frac{1}{2}$ about the origin. Is the image congruent?	Q'(4,5), R'(5,5), S'(4,13/2); no, it is not congruent.
4	Triangle JKL has J(-7,6), K(-9,6), and L(-8,8). Rotate it 180° about the origin. State whether orientation and congruence are preserved.	J'(7,-6), K'(9,-6), L'(8,-8); orientation and congruence are preserved.

PART 2 • APPLY IT

- A'(2,3), B'(5,3), C'(3,6); yes, it is congruent.** Change each x-coordinate to its opposite. A reflection preserves lengths and angle measures.
- U'(3,-6), V'(6,-6), W'(3,-3); orientation is preserved.** Multiply every coordinate by $\frac{3}{2}$. A positive dilation keeps orientation, but the image is not congruent because the scale factor is not 1.

CHALLENGE

A''(1,0), B''(-2,0), C''(-1,3); the final image is congruent, and its orientation is reversed.

Accept coordinates written as ordered pairs in any clear equivalent format. For orientation, accept "reversed" or "changes" for a reflection, and "preserved" or "same" for translations, rotations, and positive dilations.