

Coordinate Motion Lab

Use rules to move points on a coordinate plane.

GRADE 8 • TEKS 8.10.C

8.10.C "explain the effect of translations, reflections over the x- or y-axis, and rotations limited to 90° , 180° , 270° , and 360° as applied to two-dimensional shapes on a coordinate plane using an algebraic representation; and"

NAME _____

DATE _____

RULES FOR MOVING POINTS

Use an ordered-pair rule to show what happens to each vertex. A translation adds or subtracts from coordinates, and reflections use $(x, y) \rightarrow (x, -y)$ over the x-axis or $(x, y) \rightarrow (-x, y)$ over the y-axis. About the origin, 90° counterclockwise is $(x, y) \rightarrow (-y, x)$, 180° is $(x, y) \rightarrow (-x, -y)$, 270° counterclockwise is $(x, y) \rightarrow (y, -x)$, and 360° leaves a point unchanged.

WORKED EXAMPLE

Point M(7, -8) is translated by the rule $(x, y) \rightarrow (x + 4, y + 9)$. Find M'.

1. Start with M(7, -8).
2. Add 4 to the x-coordinate: $7 + 4 = 11$.
3. Add 9 to the y-coordinate: $-8 + 9 = 1$.

Answer: M'(11, 1)

PRACTICE 5 problems

- 1** Translate Q(-2, 3) by the rule $(x, y) \rightarrow (x - 3, y + 2)$. Find Q'.

ANSWER _____

- 2** Reflect R(3, -6) over the x-axis. Find R'.

ANSWER _____

- 3** Reflect S(-5, 2) over the y-axis. Find S'.

ANSWER _____

- 4** Rotate T(2, -6) 90° counterclockwise about the origin. Find T'.

ANSWER _____

- 5** Rotate U(-6, 3) 180° about the origin. Find U'.

ANSWER _____

APPLY IT Show your work

- 1** A video game designer rotates a triangular logo 270° counterclockwise about the origin. Its vertices are $A(-6, 2)$, $B(-5, 3)$, and $C(-3, 5)$. What are the coordinates of A' , B' , and C' ?

WORK SPACE

ANSWER _____

- 2** A robotics team moves a triangular sensor zone using the rule $(x, y) \rightarrow (x - 3, y + 2)$. The vertices are $D(6, -5)$, $E(3, -5)$, and $F(6, -2)$. What are the new coordinates?

WORK SPACE

ANSWER _____

CHALLENGE One step up

Point $P(x, y)$ is reflected over the x -axis and then rotated 180° about the origin. Write the final ordered-pair rule. Explain why this result is the same as one reflection.

WORK SPACE AND ANSWER

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	Translate Q(-2, 3) by the rule $(x, y) \rightarrow (x - 3, y + 2)$. Find Q'.	Q'(-5, 5)
2	Reflect R(3, -6) over the x-axis. Find R'.	R'(3, 6)
3	Reflect S(-5, 2) over the y-axis. Find S'.	S'(5, 2)
4	Rotate T(2, -6) 90° counterclockwise about the origin. Find T'.	T'(6, 2)
5	Rotate U(-6, 3) 180° about the origin. Find U'.	U'(6, -3)

PART 2 • APPLY IT

1. **A'(2, 6), B'(3, 5), C'(5, 3)** Use the 270° counterclockwise rule $(x, y) \rightarrow (y, -x)$ on each vertex.
2. **D'(3, -3), E'(0, -3), F'(3, 0)** Subtract 3 from each x-coordinate and add 2 to each y-coordinate.

CHALLENGE

$(-x, y)$. Reflecting over the x-axis gives $(x, -y)$. A 180° rotation gives $(-x, y)$, which is the same result as reflecting the original point over the y-axis.

Accept ordered pairs with or without point labels. For the challenge, accept any correct explanation that identifies the final rule as a reflection over the y-axis.