

Factor Matchup

Sort complete prime factorizations from incomplete ones.

5.NS.2.c "Determine the prime factorization for a whole number up to 100."

NAME _____

DATE _____

COMPLETE PRIME FACTORIZATION

A complete prime factorization has only prime numbers as factors. The factors multiply to the original number.

$$70 = 2 \times 5 \times 7$$

INCOMPLETE FACTORIZATION

An incomplete factorization has at least one composite number as a factor. Break the composite factor into prime factors to finish it.

$$72 = 8 \times 3 \times 3$$

1 SORT _____ 8 items

For each equation, circle COMPLETE or INCOMPLETE, then choose two items and explain how you knew each choice.

1. $54 = 2 \times 3 \times 3 \times 3$

COMPLETE

INCOMPLETE

2. $48 = 6 \times 2 \times 2 \times 2$

COMPLETE

INCOMPLETE

3. $75 = 15 \times 5$

COMPLETE

INCOMPLETE

4. $98 = 2 \times 7 \times 7$

COMPLETE

INCOMPLETE

5. $60 = 2 \times 2 \times 3 \times 5$

COMPLETE

INCOMPLETE

6. $81 = 3 \times 3 \times 3 \times 3$

COMPLETE

INCOMPLETE

7. $56 = 7 \times 4 \times 2$

COMPLETE

INCOMPLETE

8. $45 = 3 \times 3 \times 5$

COMPLETE

INCOMPLETE

2 PROVE IT Explain your thinking

Pick two items from Part 1. For each one, tell how you knew where it belonged.

ITEM # _____ HOW I KNEW _____

ITEM # _____ HOW I KNEW _____

3 MAKE YOUR OWN One of each

Write one new COMPLETE example and one new INCOMPLETE example. Each equation must equal the number on the left.

COMPLETE _____

INCOMPLETE _____

CHALLENGE

Write the complete prime factorization of 96. Then write a different factorization of 96 that is incomplete because it has a composite factor.

PART 1 • SORT

#	ITEM	CATEGORY	WHY
1	$54 = 2 \times 3 \times 3 \times 3$	COMPLETE	All factors are prime, and $2 \times 3 \times 3 \times 3 = 54$.
2	$48 = 6 \times 2 \times 2 \times 2$	INCOMPLETE	The factors equal 48, but 6 is composite.
3	$75 = 15 \times 5$	INCOMPLETE	The factors equal 75, but 15 is composite.
4	$98 = 2 \times 7 \times 7$	COMPLETE	All factors are prime, and $2 \times 7 \times 7 = 98$.
5	$60 = 2 \times 2 \times 3 \times 5$	COMPLETE	All factors are prime, and $2 \times 2 \times 3 \times 5 = 60$.
6	$81 = 3 \times 3 \times 3 \times 3$	COMPLETE	All factors are prime, and $3 \times 3 \times 3 \times 3 = 81$.
7	$56 = 7 \times 4 \times 2$	INCOMPLETE	The factors equal 56, but 4 is composite.
8	$45 = 3 \times 3 \times 5$	COMPLETE	All factors are prime, and $3 \times 3 \times 5 = 45$.

PART 2 • PROVE IT

Accept any explanation that names the deciding feature from the rule box for the chosen item.

PART 3 • MAKE YOUR OWN (SAMPLE ANSWERS)

- **COMPLETE:** $84 = 2 \times 2 \times 3 \times 7$
- **INCOMPLETE:** $90 = 9 \times 2 \times 5$

Challenge: $96 = 2 \times 2 \times 2 \times 2 \times 2 \times 3$. An incomplete factorization is $96 = 12 \times 2 \times 2 \times 2$ because 12 is composite.

COMPLETE: 1, 4, 5, 6, 8. INCOMPLETE: 2, 3, 7. For explanations, students should identify the composite factor in incomplete equations or verify that every factor is prime in complete equations.