

Angle Detective

Use quadrilateral clues to find missing angles.

GRADE 7 • 7.MG.3.c

7.MG.3.c "Given a diagram, determine an unknown angle measure in a quadrilateral, using properties of quadrilaterals."

NAME _____

DATE _____

THE BIG IDEA

The four interior angles of any quadrilateral add to 360 degrees. In a parallelogram, opposite angles are equal, and angles next to each other add to 180 degrees. Read the diagram markings before choosing a rule.

WORKED EXAMPLE

Diagram: W-----X / \ Z-----Y
 $m\angle W = 105$ degrees, $m\angle Y = 88$ degrees, $m\angle Z = 73$ degrees, and $m\angle X = x$. Find x .

1. Add the known angles: $105 + 88 + 73 = 266$.
2. Subtract from the total: $360 - 266 = 94$.
3. $m\angle X = 94$ degrees, so $x = 94$.

Answer: 94 degrees

PRACTICE 6 problems

- 1** Diagram: A-----B / \ D-----C $m\angle A = 110$ degrees, $m\angle B = 95$ degrees, $m\angle C = 70$ degrees, and $m\angle D = x$. Find $m\angle D$.

ANSWER _____

- 2** Diagram, parallelogram ABCD: A-----B / / D-----C $AB \parallel DC$ and $AD \parallel BC$ $m\angle A = 128$ degrees and $m\angle B = x$. Find $m\angle B$.

ANSWER _____

- 3** Diagram, rectangle EFGH: E-----F || H-----G
 All four corners have right-angle marks.
 $m\angle F = x$. Find x .

ANSWER _____

- 4** Diagram, trapezoid JKLM: J-----K \ \ M-----L
 $JK \parallel ML$ $m\angle J = 67$ degrees and $m\angle M = x$.
 Find $m\angle M$.

ANSWER _____

- 5** Diagram, rhombus PQRS: P / \ S Q \ / R $m\angle P = 72$ degrees and $m\angle R = x$. Find $m\angle R$.

ANSWER _____

- 6** Diagram: A-----B / \ D-----C $m\angle A = x + 22$ degrees, $m\angle B = 106$ degrees, $m\angle C = 79$ degrees, and $m\angle D = 63$ degrees. Find $m\angle A$ and x .

ANSWER _____

APPLY IT Show your work

- 1** Jada makes a slanted frame for her gaming channel thumbnail. The frame is a parallelogram PQRS. Diagram: P-----Q // S-----R $PQ \parallel SR$ and $PS \parallel QR$ $m\angle P = 124$ degrees and $m\angle Q = x$. What is $m\angle Q$?

WORK SPACE

ANSWER _____

- 2** A skate park designer draws a ramp sign shaped like trapezoid JKLM. The top and bottom edges are parallel. Diagram: J-----K \ \ M-----L $JK \parallel ML$ $m\angle J = 74$ degrees and $m\angle M = x$. What is $m\angle M$?

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

Diagram, parallelogram ABCD: A-----B // D-----C $AB \parallel DC$ and $AD \parallel BC$ $m\angle A = 3x + 12$ degrees and $m\angle C = 5x - 26$ degrees. Find x and $m\angle B$. Explain how the diagram helps you.

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	Diagram: A-----B / \ D-----C $m\angle A = 110$ degrees, $m\angle B = 95$ degrees, $m\angle C = 70$ degrees, and $m\angle D = x$. Find $m\angle D$.	85 degrees
2	Diagram, parallelogram ABCD: A-----B // D-----C $AB \parallel DC$ and $AD \parallel BC$ $m\angle A = 128$ degrees and $m\angle B = x$. Find $m\angle B$.	52 degrees
3	Diagram, rectangle EFGH: E-----F H-----G All four corners have right-angle marks. $m\angle F = x$. Find x .	90 degrees
4	Diagram, trapezoid JKLM: J-----K \ \ M-----L $JK \parallel ML$ $m\angle J = 67$ degrees and $m\angle M = x$. Find $m\angle M$.	113 degrees
5	Diagram, rhombus PQRS: P / \ S Q \ / R $m\angle P = 72$ degrees and $m\angle R = x$. Find $m\angle R$.	72 degrees
6	Diagram: A-----B / \ D-----C $m\angle A = x + 22$ degrees, $m\angle B = 106$ degrees, $m\angle C = 79$ degrees, and $m\angle D = 63$ degrees. Find $m\angle A$ and x .	$m\angle A = 112$ degrees, $x = 90$

PART 2 • APPLY IT

- 56 degrees** Angles next to each other in a parallelogram add to 180 degrees. $180 - 124 = 56$.
- 106 degrees** Angles on the same leg between parallel sides add to 180 degrees. $180 - 74 = 106$.

CHALLENGE

$x = 19$ and $m\angle B = 111$ degrees. Opposite angles in a parallelogram are equal, so $3x + 12 = 5x - 26$. Then $m\angle A = 69$ degrees, and $m\angle B = 180 - 69 = 111$ degrees.

Accept answers written with a degree symbol or the word degrees. For the algebra items, accept the requested angle measure and x value when both are correct.