

Solid Shape Sprint

Find volume and surface area of 3D shapes.

GRADE 8 • 8.MG.2.d

8.MG.2.d "Solve problems in context involving volume of cones and square-based pyramids and the surface area of square-based pyramids."

NAME _____

DATE _____

VOLUME AND SURFACE AREA

For a cone, $V = \frac{1}{3} \pi r^2 h$. For a square-based pyramid, $V = \frac{1}{3} s^2 h$ and $SA = s^2 + 2sl$. Use vertical height h for volume and slant height l for the triangular faces in surface area.

WORKED EXAMPLE

Find the volume of a cone with radius 4 cm and vertical height 15 cm.

$$1. V = \frac{1}{3} \pi r^2 h$$

$$2. V = \frac{1}{3} \pi (4^2)(15)$$

$$3. V = \frac{1}{3} \pi (16)(15) = 80\pi$$

Answer: $80\pi \text{ cm}^3$

PRACTICE 6 problems

- 1** Find the volume of a cone with radius 3 cm and vertical height 8 cm. Leave your answer in terms of π .

ANSWER _____

- 2** Find the volume of a cone with radius 6 cm and vertical height 5 cm. Leave your answer in terms of π .

ANSWER _____

- 3** Find the volume of a square-based pyramid with base side length 7 cm and vertical height 9 cm.

ANSWER _____

- 4** Find the total surface area of a square-based pyramid with base side length 10 cm and slant height 13 cm.

ANSWER _____

- 5** Find the volume of a square-based pyramid with base side length 12 cm and vertical height 11 cm.

ANSWER _____

- 6** Find the total surface area of a square-based pyramid with base side length 5 cm and slant height 7 cm.

ANSWER _____

APPLY IT Show your work

- 1** A student in the maker club is building a solid cone-shaped rocket nose from foam. The nose has a radius of 9 cm and a vertical height of 10 cm. What is its volume? Leave your answer in terms of pi.

WORK SPACE

ANSWER _____

- 2** The art club is making a square-pyramid trophy cover from cardboard. Its base side length is 14 cm, and the slant height of each triangular face is 8 cm. How much cardboard is needed to cover all five faces, including the base?

WORK SPACE

ANSWER _____

CHALLENGE One step up

CHALLENGE

A right square-based pyramid has a volume of 384 cm^3 and a vertical height of 8 cm. Its slant height is 10 cm. Find the base side length, then find the total surface area.

PART 1 • PRACTICE

#	PROBLEM	ANSWER
1	Find the volume of a cone with radius 3 cm and vertical height 8 cm. Leave your answer in terms of pi.	24pi cm³
2	Find the volume of a cone with radius 6 cm and vertical height 5 cm. Leave your answer in terms of pi.	60pi cm³
3	Find the volume of a square-based pyramid with base side length 7 cm and vertical height 9 cm.	147 cm³
4	Find the total surface area of a square-based pyramid with base side length 10 cm and slant height 13 cm.	360 cm²
5	Find the volume of a square-based pyramid with base side length 12 cm and vertical height 11 cm.	528 cm³
6	Find the total surface area of a square-based pyramid with base side length 5 cm and slant height 7 cm.	95 cm²

PART 2 • APPLY IT

- 270pi cm³** Use $V = \frac{1}{3} \pi r^2 h$. Substitute 9 for r and 10 for h: $\frac{1}{3} \pi (9^2)(10) = 270\pi \text{ cm}^3$.
- 420 cm²** Use $SA = s^2 + 2sl$. The base area is $14^2 = 196 \text{ cm}^2$, and the four triangular faces have area $2(14)(8) = 224 \text{ cm}^2$.

CHALLENGE

Base side length: 12 cm; total surface area: 384 cm²

Accept equivalent exact forms that keep pi, such as pi times 24. Surface-area answers must include the square base as well as all four triangular faces.